▸ MATTEO DE CEGLIE, *The V-logic multiverse and MAXIMIZE.*
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I argue that classical set theory, $ZFC(+LCs)$, is *restrictive* compared to the V-logic multiverse (a novel set theoretic multiverse developed by the author and Claudio Ternullo). This multiverse is based upon Friedman's Hyperuniverse and Steel's set-generic multiverse: like the Hyperuniverse, it uses the infinitary V-logic as background logic (this logic admits formulas of length less than the first successor of the least inaccessible cardinal, but only a finite block of quantifiers in front of them) and admits all kinds of outer models of V (produced by set-generic, class-generic, hyperclass forcing). Like Steel's set-generic multiverse, it is recursively axiomatisable and is rooted on a ground universe that satisfies ZFC. For this proof, I compare $ZFC+LCs$ and the V-logic multiverse, characterised as $ZFC + LCs+$ the Multiverse Axiom Schema (this axiom tells us that if a sentence φ is consistence in V-logic then there is an actual outer model of V satisfying it), following Maddy's methodological principle MAXIMIZE (introduced in [3]). According to this principle, when comparing two foundational theories we should prefer the one that can prove more isomorphism types. I claim that the V-logic multiverse, as opposed to $ZFC + LCs$, does exactly that. This is because in the V-logic multiverse theory we can prove the existence of proper, uncountable, extensions of V, that we cannot have in $ZFC + LCs$ (see [2]). In turn, these extra objects means we can realise more isomorphism types that are not available in $ZFC + LCs$, since in the V-logic multiverse we can prove the existence of iterable class sharps and, more importantly, maps between them (see [1]). Moreover, when moving from $ZFC + LCs$ to the V-logic Multiverse we are not losing anything: ZFC, all the large cardinals, inner models and V are still there. On the other hand, when moving from the V-logic multiverse to $ZFC + LCs$ we lose the actual outer models of V, iterable class sharps and iterable class sharp generated models. Thus, this latter theory is restrictive compared to the V-logic multiverse theory.

[1] Carolin Antos, Neil Barton, Sy-David Friedman, *Universism and extensions of V*, ***Review of Symbolic Logic***, FirstView (forthcoming), pp. 1–43.

[2] Neil Barton, *Forcing and the Universe of Sets: Must we lose insight?*, ***Journal of Philosophical Logic***, vol. 49 (2020), no. 4, pp. 575–612.

[3] Penelope Maddy, ***Naturalism in Mathematics***, Oxford University Press, 1998.